

Biometry. Lecture 19

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1 Two-dimensional statistics

- Linear models
- Analysis of covariation



```
> setwd("<working folder>")  
or  
"Change dir"  
in menu!
```

On Mac, be sure that startup option is working: `getwd()`
(`getwd()` checks if R is in working folder, `dir()` checks the folder content)



Two-dimensional statistics

Linear models



Diagnostic plots again: good Residuals vs. Fitted

```
> par(mfrow = c (3, 3))  
> set.seed(101)  
> for (i in 1:9) plot(1:50, rnorm(50), xlab="Fitted",  
+ ylab = "Residuals")
```

Dispersion of residuals is homogeneous.



Diagnostic plots again: bad Residuals vs. Fitted

```
> par(mfrow = c (3, 3))  
> set.seed(102)  
> for (i in 1:9) plot(1:50, (1:50)*rnorm(50), xlab="Fitted",  
+ ylab = "Residuals")
```

Dispersion of residuals is **not** homogeneous.



Women model again: adding squared term

```
> women.lm1 <- lm(weight ~ height, data=women)
> women.lm2 <- lm(weight ~ height + I(height^2), data=women)
> summary(women.lm2)
> plot(women.lm1, which=1)
> plot(women.lm2, which=1) # much better!
```



One more model

- We will try to understand the relation between gross state product (GDP) and rate of murders



One more model, part I

```
> gdp2010 <- read.table("
+ http://ashipunov.info/data/gdp2010.txt", h=T, sep="\t")
> mg <- data.frame(murder=USArrests$Murder,
+ gdp=gdp2010$GDP)
> mg.lm <- lm(murder ~ gdp, data=mg)
> summary(mg.lm)
> plot(mg.lm) # NOT a plot of model: 4 diagnostic plots
> plot(murder ~ gdp, data=mg) # Plot of model
> abline(mg.lm)
```

If 1st and 3rd quartiles are too far from median, residuals could be over-dispersed.

In model formula, dependent variable is always a first one, independent variable(s) are after tilde.

We may call the slope significant only if we stated **before** the analysis that the threshold will be 0.1 like it is normal for social sciences



One more model, part II

```
> new.points <- seq(min(mg$gdp), max(mg$gdp),  
+ length.out=50)  
> new.frame <- data.frame(gdp=new.points)  
> predicted.points <- predict(mg.lm, int="c",  
+ newdata=new.frame)  
> matlines(new.points, predicted.points)  
# If you like to see names of states  
> identify(mg$gdp, mg$murder, labels=row.names(gdp2010))  
# Do not forget to click the right mouse button  
# The other way to see names of states:  
> plot(murder ~ gdp, data=mg, type="n")  
> text(y=mg$murder, x=mg$gdp, labels=row.names(gdp2010))
```



Two-dimensional statistics

Analysis of covariation



Analysis of covariation (ANCOVA)

- ANCOVA integrates several regression lines together and checks the full model
- Model formula is
$$\text{response} \sim \text{influence} * \text{factor}$$
- The ANCOVA will check if there is any difference between intersection and slope of the first line and intersections and slopes of all other lines (each line corresponds with one factor level)



Grazing data

- 40 plants were treated in two groups: with grazing (in first two weeks) and without grazing
- Rootstock diameter was also measured
- At the end of season, fruit production was measured (dry weight in mg)



Visualization first

```
> ipo <- read.table(  
+ "http://ashipunov.info/data/ipomopsis.txt", h=T)  
> head(ipo)  
> with(ipo, plot(Root, Fruit,  
+ pch=as.numeric(Grazing)))  
> abline(lm(Fruit ~ Root, data=subset(ipo,  
+ Grazing=="Grazed")))  
> abline(lm(Fruit ~ Root, data=subset(ipo,  
+ Grazing=="Ungrazed")), lty=2)  
> legend("topleft", lty=1:2,  
+ legend=c("Grazed", "Ungrazed"))
```



Model output

```
> ipo.lm <- lm(Fruit ~ Root * Grazing, data=ipo)
> summary(ipo.lm)
```

Two equations:

$\text{Fruit} = -125.174 + 23.24 * \text{Root}$ (for grazed)

$\text{Fruit} = (-125.174 + 30.806) + (23.24 + 0.756) * \text{Root}$ (for ungrazed)



Finishing...

Save your commands!

`(savehistory(<todaysdate>.r) or File -> Save as... on Mac)`



Summary: most important commands

- `lm()`—estimates the linear regression model and many other models (like ANCOVA)
- `predict()`—predict values with model



For Further Reading



A. Shipunov.

Biometry [Electronic resource].

2012—onwards.

Mode of access:

http://ashipunov.info/shipunov/school/biol_240



A. Shipunov, and others.

Visual statistics. Use R!

Ongoing translation from Russian.

