

Biometry. Lecture 11

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Outline

- 1 Questions and answers
- 2 One-dimensional data
 - Central tendency
 - Range
 - One-dimensional tests

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Starting...

```
> setwd("<working folder>")  
or  
"Change dir"  
in menu!
```

Previous final question: the answer

How to select from data frame `eq` column which name is
`NUM.Z`?

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How to select from data frame `eq` column which name is
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- `eq[, "NUM.Z"]`
- `eq$NUM.Z`

One-dimensional data

Central tendency

Mean and median

- These are two most frequently used characteristics of the central tendency.
- Median is more robust than mean.

Mean and median

```
> salary <- c(21, 19, 27, 11, 102, 25, 21)
> mean(salary); median(salary)
> median(1:3); median(1:4)
```

When number of elements is odd, median is a central value; if even—median is the average between two centrals.

Median is the third quartile

Quartiles take out 0% (minimum, `min()`), 25% (lower hinge), 50%, 75% (upper hinge) and 100% (maximum, `max()`) of ordered data. Median is simply a 50% (third) quartile.

```
> fivenum(salary)
```

Mode

Mode is the most frequent value:

```
> sex <- c("m", "f", "m", "m", "f", "m", "m")  
> t.sex <- table(sex)  
> mode <- t.sex[which.max(t.sex)]  
> mode
```

How to calculate means for all columns

```
> sapply(trees, mean)
```

Commands of `*apply()` family (`sapply()`, `apply()`, `by()`, `tapply()`) are most powerful in R

One-dimensional data

Range

Standard deviation, variance and IQR

- Variance is a sum of square differences between each value and mean divided by number of degrees of freedom (so-called “Bessel’s correction”)
- Standard deviation is a square root from variance
- IQR (inter-quartile range) is simply a difference between fourth and second quartiles. It is more robust than standard deviation.

Standard deviation, variation and IQR

```
> sd(salary); var(salary); IQR(salary)
```

Coefficient of variation

Coefficient of variation (CV) is a standardized (by mean) standard deviation

```
> cv.trees <- 100*apply(trees, sd)/colMeans(trees)
> cv.trees
```

“Volume” variable variates most.

Boxplots

Boxplots (invented by John Tukey) are one of the best representations of data central tendency and range.

```
> boxplot(salary)
> boxplot(trees)
```

Boxplots do not show mean and standard deviation.

Histograms

Histograms show the frequency of every data interval:

```
> hist(salary)
> hist(trees[,1])
```

Density plots

Density plot smooths the histogram:

```
> plot(density(trees[,3]))  
> plot(density(rnorm(1000))) # 1000000 is even better!
```

Density plots looks prettier but may lead to wrong conclusions especially if sample is small.

summary()

summary() is a “smart” (generic) function which gives the most appropriate description of data. In many cases, it will give quantiles + mean:

```
> summary(salary)
> summary(trees)
> summary(sex)
```

summary() and “bad” data

summary() is very useful when one needs to check a reliability of data:

```
> err <- read.table("http://ashipunov.info/data/errors.txt",  
+ h=TRUE, sep="^")  
> str(err)  
> summary(err)
```

AGE became a factor (erroneous “a”), empty name (instead of NA), and impossible minimal height.

One-dimensional data

One-dimensional tests

t-test and Wilcoxon test for one-dimensional data

- Statistical tests allow to check how well the general characteristic (central tendency or range) calculated from *sample* represents a *population*
- t-test (Student's) takes into account the normality of sample whereas Wilcoxon test do not consider the distribution, it is non-parametric
- Both give a *confidence interval*

t-test for one variable

```
> t.test(salary, mu=mean(salary))  
One Sample t-test  
  
data:  salary  
t = 0, df = 6, p-value = 1  
alternative hypothesis: true mean is not equal to 32.28571  
95 percent confidence interval:  
  3.468127 61.103302  
sample estimates:  
mean of x  
  32.28571
```

Understanding the test output: theory

- Alternative hypothesis (“something”) and null hypothesis (“nothing”)
- Type I error (false alarm), p-value (probability to issue the false alarm) and significance level (matter of agreement)

Understanding the test output: quick and dirty

- Which hypothesis is null?
- Does p-value less than 0.05?
 - 1 No: accept the null hypothesis—sit and relax
 - 2 Yes: reject the null hypothesis—jump and call the police

Finishing...

```
> savehistory("20120217.r")
```

Final question (2 points)

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What is a main practical difference between mean and median?

Summary: most important commands

- `median()` — returns a median value
- `IQR()` — returns robust range
- `boxplot()` — draws a boxplot
- `t.test()` — checks the reliability of mean (assuming that data distribution is normal)

For Further Reading



A. Shipunov.

Biometry [Electronic resource].

2012—onwards.

Mode of access: [http:](http://ashipunov.info/shipunov/school/biol_299)

[//ashipunov.info/shipunov/school/biol_299](http://ashipunov.info/shipunov/school/biol_299)



P. Dalgaard

Introductory Statistics with R. 2nd edition.

Springer, 2008.

Chapters 4, 5:1–2.